

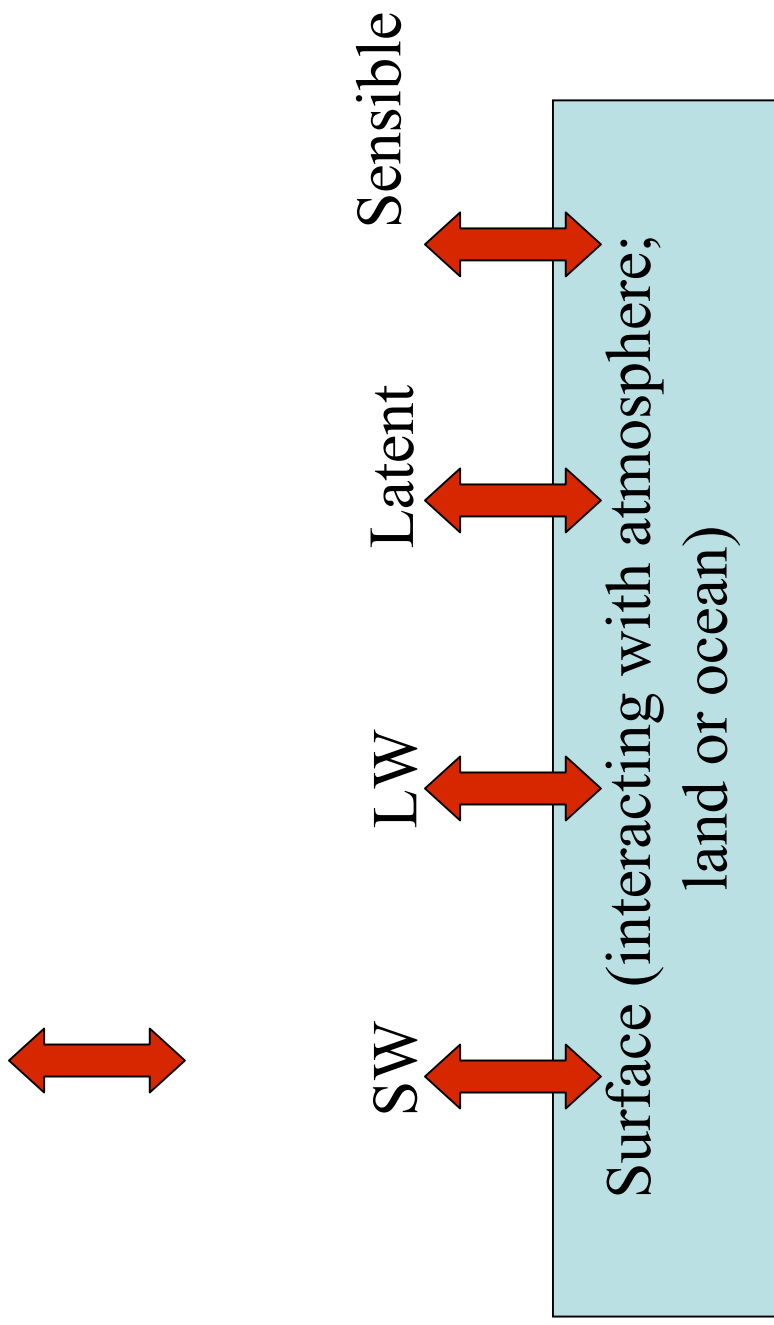
# Surface energy balance I

Reading: GPC Ch4

Outline:

- Surface energy budget
- Surface heat storage, penetration depth
- Radiative flux at the surface - SW and LW

# The energy balance at the surface



## 4.2 Surface energy budget

$$\frac{\partial E_s}{\partial t} = G = R_s - LE - SH - \Delta F_{eo}$$

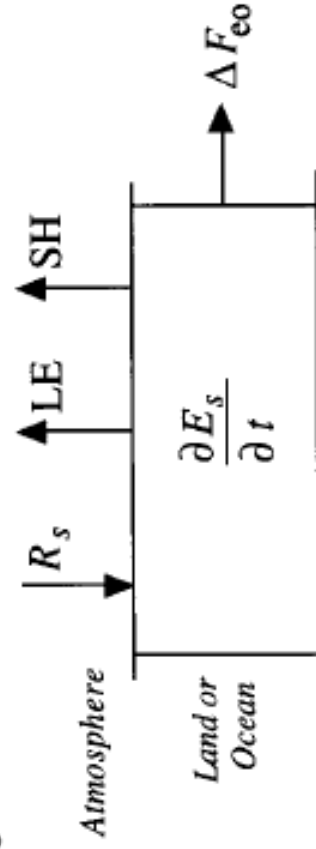
Total radiation

Latent heat flux

Sensible heat flux

Horizontal energy flux

Storage of energy in surface



Energy balance

$$R_s = LE + SH + \Delta F_{eo}$$



## **Heat storage at the surface**

It is important for the seasonal cycle of T over the oceans and for the diurnal cycle over land and oceans.

The amount of energy in the surface box ( $/m^2$ ) may be written as  $E_s = C_e T_e$  where  $C_e$  is the effective heat capacity of the medium and  $T_e$  is the effective temperature of the energy storing medium.

## ***Comparison between atmosphere and ocean***

Thermal capacity of atmosphere,  $C_a$

$$\begin{aligned} &= c_p \times \text{mass of atm. per unit area} \\ &= c_p p_s / g = 1.02 \times 10^7 \text{ J K}^{-1} \text{ m}^{-2} \end{aligned}$$

Thermal capacity of ocean depth  $d_w$ ,  $C_o$

$$\begin{aligned} &= c_w \times \text{mass of ocean per unit area} \\ &= c_w \rho_w d_w = \mathbf{d_w} \times 4.2 \times 10^6 \text{ J K}^{-1} \text{ m}^{-2} \end{aligned}$$

**(so thermal capacity of atmosphere  $\sim$  2m of water)**

**Soil:** no motions, conduction (less efficient). Typically  $C_s$  slightly smaller than that of the atmosphere. Shallow penetration depth.

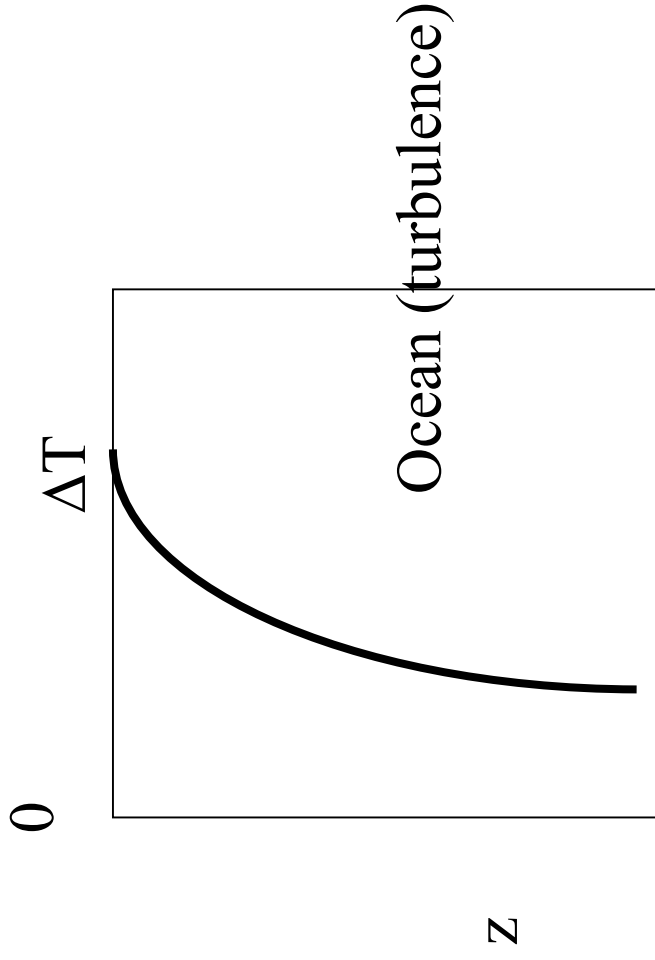
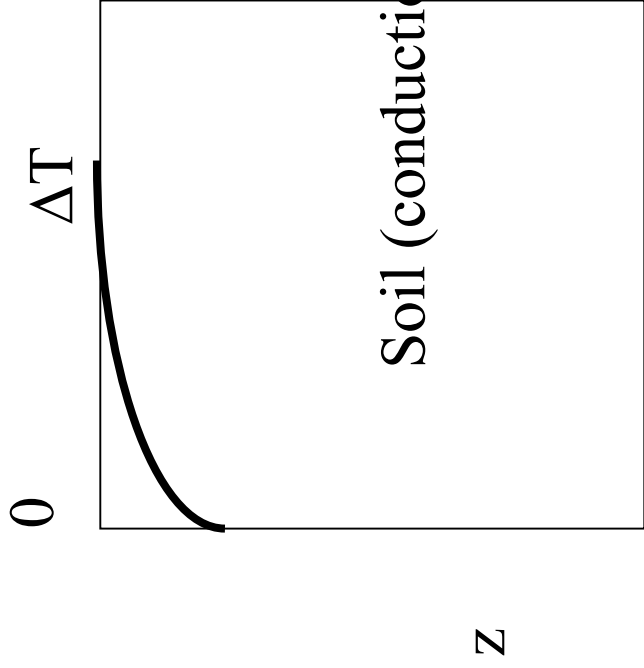
**Table 4.1**  
Properties of Soil Components at 293 K

|                         | Specific heat ( $c_p$ )<br>( $\text{J kg}^{-1} \text{K}^{-1}$ ) | Density ( $\rho$ )<br>( $\text{kg m}^{-3}$ ) | $\rho c_p$<br>( $\text{J m}^{-3} \text{K}^{-1}$ ) |
|-------------------------|---|--|---|
| Soil inorganic material | 733   | 2600   | $1.9 \times 10^6$                                 |
| Soil organic material   | 1921  | 1300   | $2.5 \times 10^6$                                 |
| Water                   | 4182  | 1000   | $4.2 \times 10^6$                                 |
| Air                     | 1004  | 1.2  | $1.2 \times 10^3$                                 |

[After Brutsaert (1982). Reprinted with permission from Kluwer Academic Publishers.]

When water replaces air in the open spaces of the soil (porosity)  $c_p$  increases.  
 $\rho c_p$  = volumetric heat capacity

## Heat storage in the soil



Land has a smaller overall heat capacity relative to ocean mainly because the penetration depth is shallower. Heat is transferred downwards by *conduction* over land and turbulent mixing (convection) in the ocean surface layer.

The **penetration depth** determines what depth of ocean/land is relevant to climate. Penetration depth (here denoted  $h_T$ ) depends on *time and thermal diffusivity*

$$D_T = \text{thermal diffusivity of surface material}$$
$$\tau = \text{characteristic time of periodic forcing at the surface}$$

Typical soil diffusivity:  $D_T = 5 \times 10^{-7} \text{m}^2 \text{s}^{-1}$   
e.g. for diurnal cycle  $\tau \sim 1$  day, so  $h_T \sim 0.2$  m  
for seasonal cycle  $\tau \sim 1$  year, so  $h_T \sim 4$  m

For ocean on seasonal timescales  $h_T \sim 70$  m.

An important point is that penetration depth goes as the time<sup>1/2</sup>.

Because of poor conduction properties, horizontal transport of energy in the soil is negligible.



How did we get this function for penetration depth?

$$F_s = -K_T \frac{\partial T}{\partial z}$$

Energy flux into soil proportional to temperature gradient

Rate of temperature change proportional to flux convergence - you've seen this before!

$$C_s \frac{\partial T}{\partial t} = -\frac{\partial}{\partial z} (F_s) = \frac{\partial}{\partial z} \left( K_T \frac{\partial T}{\partial z} \right)$$

or

$$\frac{\partial T}{\partial t} = D_T \frac{\partial^2 T}{\partial z^2}$$

where  $D_T = K_T / C_s$

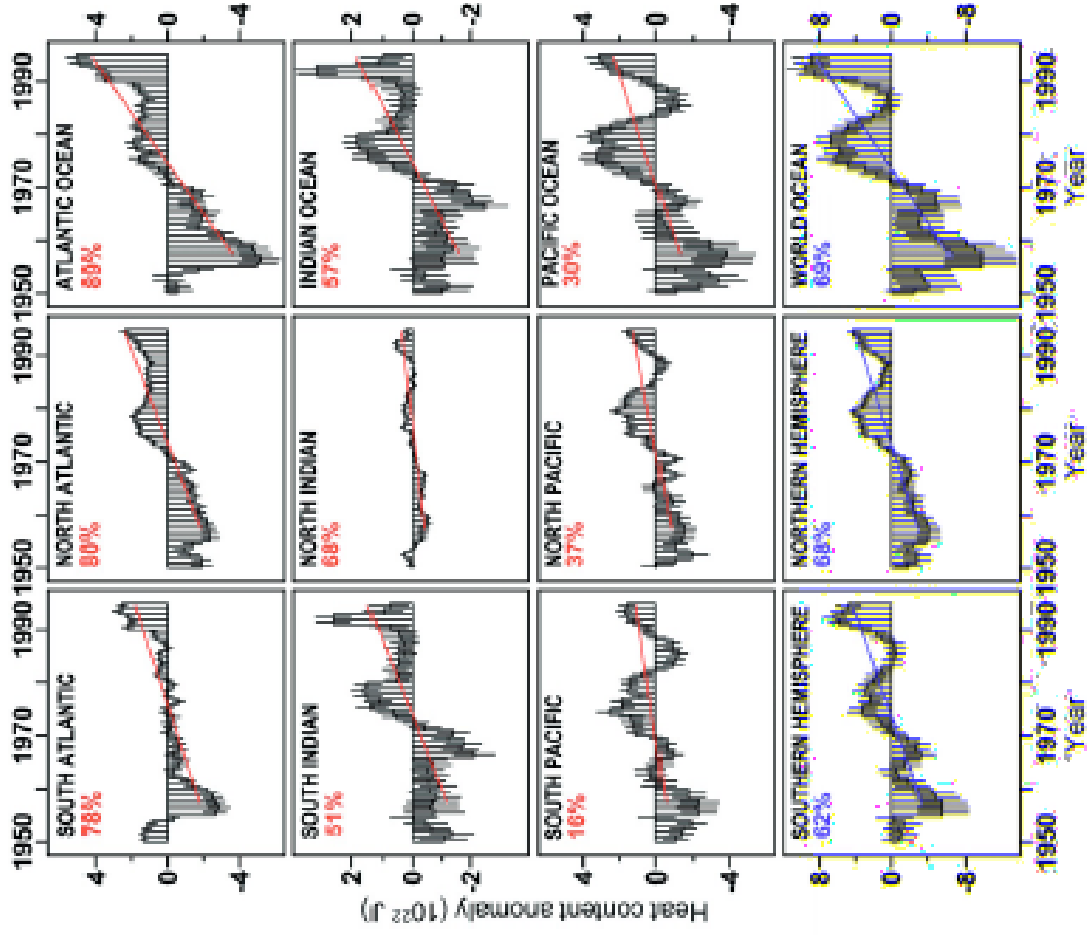
This turns out to be the heat equation, whose solution is beyond the course (you'll need to solve for the semi-infinite case with boundary conditions at the surface, and specified initial conditions).

However, a scale analysis shows that the typical depth for penetration of a surface temperature anomaly is as given as  $(D_T \tau)^{1/2}$

Levitus et al. 2000

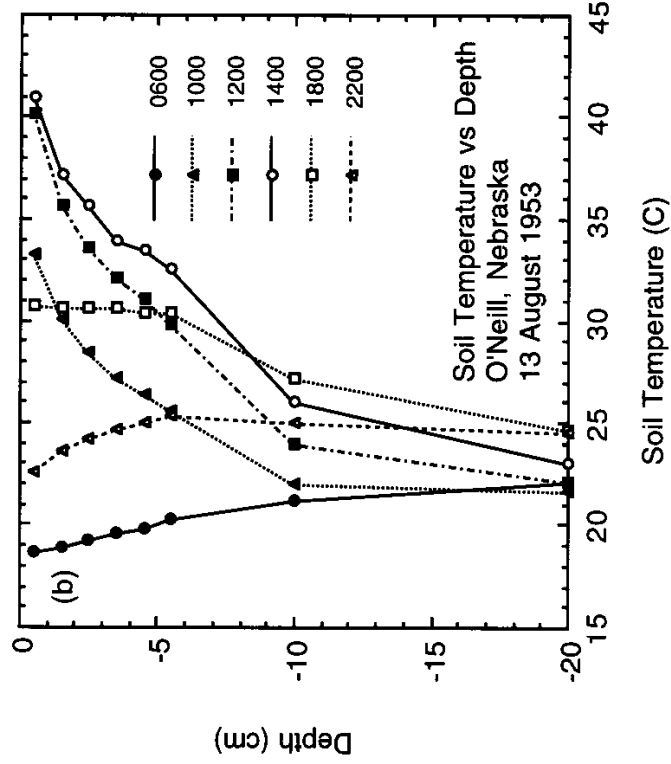
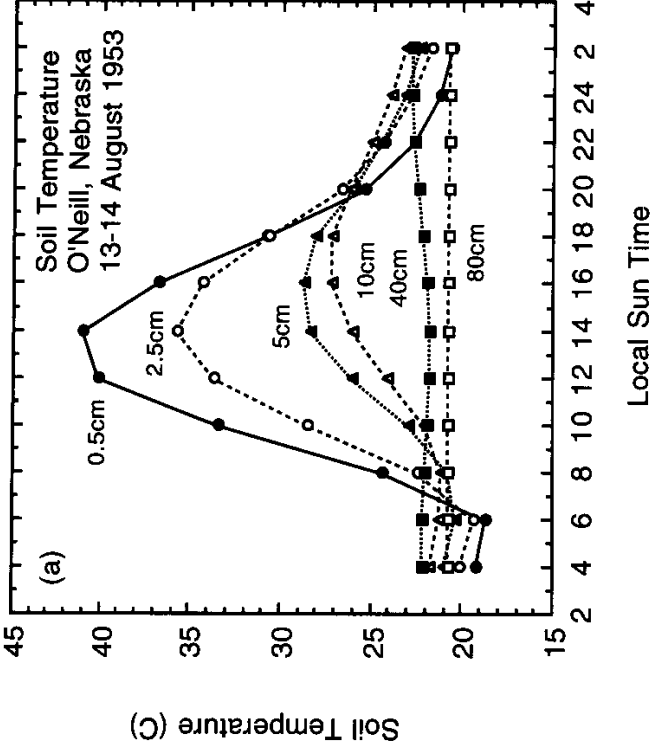
- observed heat  
content in the  
upper 3km of the  
world's oceans  
1955-1996.

Notice the increase.



Clear  
summer  
day –  
grass  
field

Soil temperatures at various depths vs. local sun time. The amplitude of the diurnal cycle decreases of  $\sim 1/e$  of the surface value at a depth of  $\sim 10$  cm and is very small below 40 cm.



Vertical profiles of soil temperature at various times of the day.

## Radiative heating of the surface

Net input of radiative energy to the surface:

$$R_s = \underbrace{S^\downarrow(0) - S^\uparrow(0)}_{\text{Net solar radiation}} + \underbrace{F^\downarrow(0) - F^\uparrow(0)}_{\text{Net LW radiation}} \quad (\text{flux densities})$$

$$S^\downarrow(0) - S^\uparrow(0) = S^\downarrow(0)(1 - \alpha_s)$$

$\alpha_s$  = surface albedo.

Varies widely depending on surface type and conditions

$$F^\downarrow(0) - F^\uparrow(0) = \varepsilon \left( F^\downarrow(0) - \sigma T_s^4 \right)$$

$\varepsilon$  = LW emissivity of the surface ~ absorptivity

because abs. and emit. LW have about the same  $\nu$ .

A fraction  $\varepsilon$  of  $F^\downarrow(0)$  is absorbed and  $(1-\varepsilon)F^\downarrow(0)$  is re-emitted

$$\rightarrow F^\uparrow(0) = (1-\varepsilon)F^\downarrow(0) + \varepsilon\sigma T_s^4$$

**Table 4.2**

Albedos for Various Surfaces in Percent

| Surface type                         | Range | Typical value |
|--------------------------------------|-------|---------------|
| <b>Water</b>                         |       |               |
| Deep water: low wind, low altitude   | 5-10  | 7             |
| Deep water: high wind, high altitude | 10-20 | 12            |
| <b>Bare surfaces</b>                 |       |               |
| Moist dark soil, high humus          | 5-15  | 10            |
| Moist gray soil                      | 10-20 | 15            |
| Dry soil, desert                     | 20-35 | 30            |
| Wet sand                             | 20-30 | 25            |
| Dry light sand                       | 30-40 | 35            |
| Asphalt pavement                     | 5-10  | 7             |
| Concrete pavement                    | 15-35 | 20            |
| <b>Vegetation</b>                    |       |               |
| Short green vegetation               | 10-20 | 17            |
| Dry vegetation                       | 20-30 | 25            |
| Coniferous forest                    | 10-15 | 12            |
| Deciduous forest                     | 15-25 | 17            |
| <b>Snow and ice</b>                  |       |               |
| Forest with surface snowcover        | 20-35 | 25            |
| Sea ice, no snowcover                | 25-40 | 30            |
| Old, melting snow                    | 35-65 | 50            |
| Dry, cold snow                       | 60-75 | 70            |
| Fresh, dry snow                      | 70-90 | 80            |

Albedos for various surfaces - vary from 70-90% for fresh snow to 5-10% for oceans in low wind speed situations

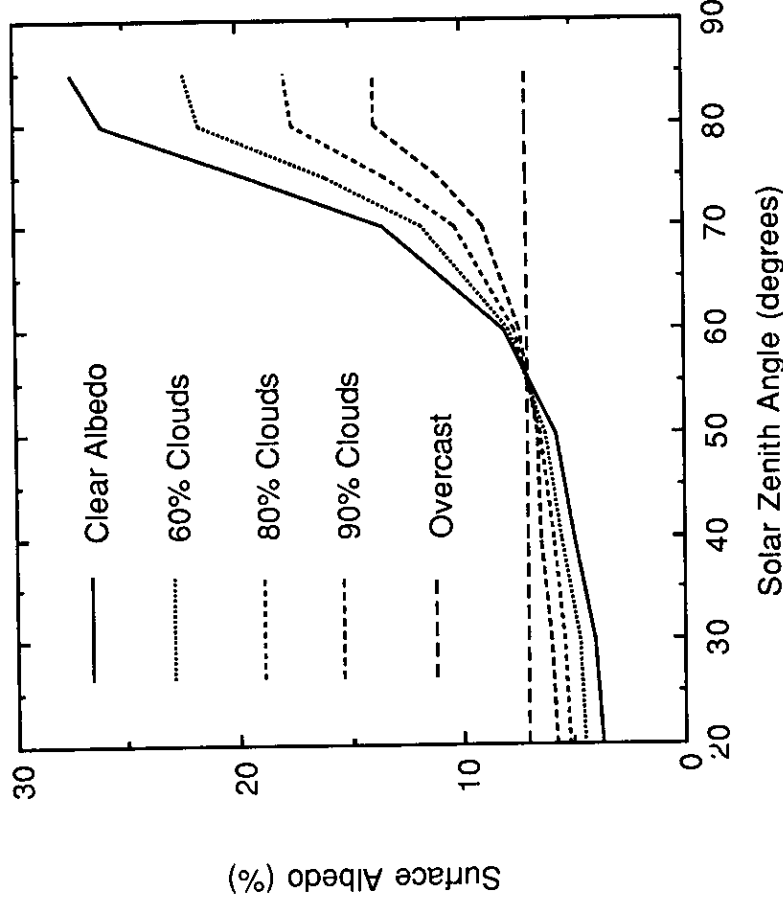
Highly variable → strong effect on absorbed LW, hence on surface T

↑ Depends on solar zenith angle too

Albedo depends on solar zenith angle

**BUT: under overcast skies, solar zenith angle matters less and less.**

Clouds scatter radiation, so that SW under a cloud is no longer a parallel beam but is scattered in all directions. Therefore as cloudiness increases the albedo becomes less and less sensitive to solar zenith angle. The amount of SW reaching the surface under overcast skies is sensitive to solar zenith angle, however, because the albedo of *clouds* depends on it.



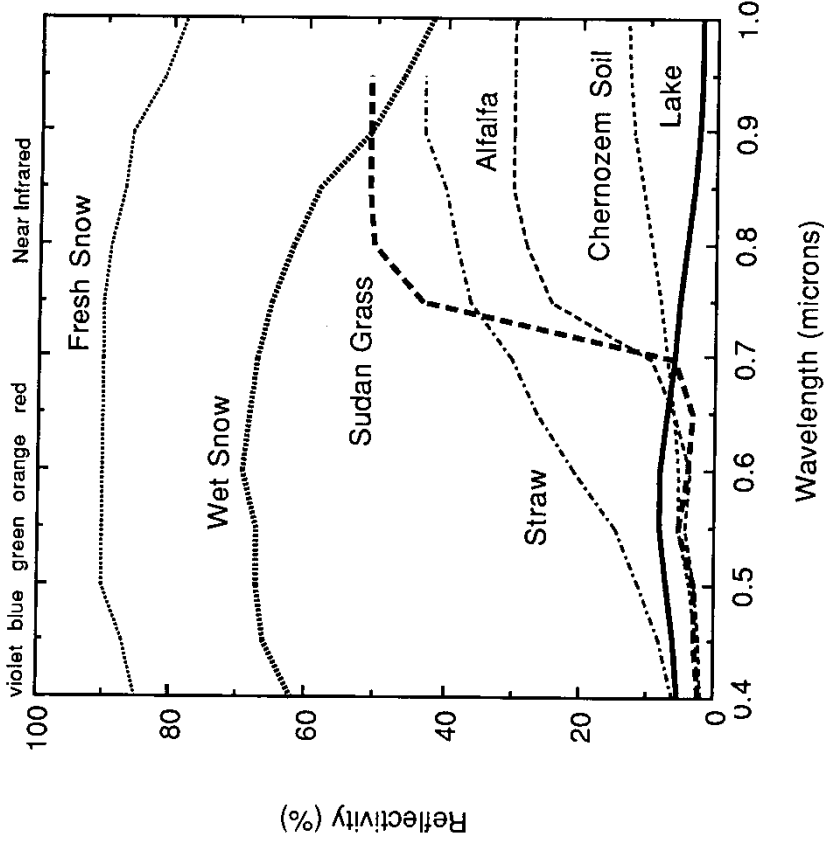
Water surface

Albedo also depends on wind speed and impurities in the water

**Fig. 4.4** Dependence of the albedo of a water surface on solar zenith angle and cloud cover. [Data from Mirinova (1973).]

Albedo also depends on frequency of SW radiation:

More reflective



Note the dip around 0.7 microns for grass and alfalfas: green plants have a very low albedo for photosynthetically-active radiation. The increase for  $\lambda > 0.7 \mu\text{m}$  helps the leaves to stay cool.

**Fig. 4.5** Surface reflectivity as a function of wavelength of radiation for a variety of natural surfaces. Human eyesight is sensitive to wavelengths from 0.4  $\mu\text{m}$  (violet) to 0.7  $\mu\text{m}$  (red). Alfalfa and sudan grass appear green because their albedo is higher for green light (~0.55  $\mu\text{m}$ ) than for other visible wavelengths. [Data from Mirinova (1973).]

Moist ground is generally darker than dry ground and therefore has a lower albedo.

**Table 4.3**  
Albedos for Dry and Moist Soil Surfaces

|                                    | Even surface |       | Tilled surface |       |
|------------------------------------|--------------|-------|----------------|-------|
|                                    | Dry          | Moist | Dry            | Moist |
| Chernozem of dark gray color       | 13           | 8     | 8              | 4     |
| Light chestnut soil of gray color  | 18           | 10    | 14             | 6     |
| Chestnut soil of grayish red color | 20           | 12    | 15             | 7     |
| Gray sandy soil                    | 25           | 18    | 20             | 11    |
| White sand                         | 40           | 20    | —              | —     |
| Dark blue clay                     | 23           | 16    | —              | —     |

[From Mironova (1973).]



# Net LW heating at the surface

$$F^{\uparrow}(0) = (1 - \epsilon)F^{\downarrow}(0) + \epsilon\sigma T_s^4$$

OR 
$$F^{\downarrow}(0) - F^{\uparrow}(0) = \epsilon(F^{\downarrow}(0) - \sigma T_s^4)$$

$\epsilon$  is the emissivity -  
generally high for  
earth surfaces  
(90%+)

$\epsilon$  inaccuracies do not play  
a key role in determining  
the surface climate because  
 $\epsilon F^{\downarrow}(0)$  and  $\epsilon\sigma T_s^4$  are both  
large and tend to offset  
each other.

Table 4.4

Infrared Emissivities (percent) of Some Surfaces

| Water and soil surfaces |         | Vegetation              |       |
|-------------------------|---------|-------------------------|-------|
| Water                   | 92-96   | Alfalfa, dark green     | 95    |
| Snow, fresh fallen      | 82-99.5 | Oak leaves              | 91-95 |
| Snow, ice granules      | 89      | Leaves and plants       |       |
| Ice                     | 96      | 0.8 $\mu\text{m}$       | 5-53  |
| Soil, frozen            | 93-94   | 1.0 $\mu\text{m}$       | 5-60  |
| Sand, dry playa         | 84      | 2.4 $\mu\text{m}$       | 70-97 |
| Sand, dry light         | 89-90   | 10.0 $\mu\text{m}$      | 97-98 |
| Sand, wet               | 95      | Miscellaneous           |       |
| Gravel, coarse          | 91-92   | Paper, white            | 89-95 |
| Limestone, light gray   | 91-92   | Glass pane              | 87-94 |
| Concrete, dry           | 71-88   | Bricks, red             | 92    |
| Ground, moist, bare     | 95-98   | Plaster, white          | 91    |
| Ground, dry plowed      | 90      | Wood, planed oak        | 90    |
| Natural surfaces        |         | Paint, white            | 91-95 |
| Desert                  | 90-91   | Paint, black            | 88-95 |
| Grass, high dry         | 90      | Paint, aluminum         | 43-55 |
| Field and shrubs        | 90      | Aluminum foil           | 1-5   |
| Oak woodland            | 90      | Iron, galvanized        | 13-28 |
| Pine forest             | 90      | Silver, highly polished | 2     |
|                         |         | Skin, human             | 95    |

[Data from Sellers (1965). Reprinted with permission from the University of Chicago Press.]